

Suresh K. Bhavnani\*, Bryant Dang, Varun Kilaru, Maria Caro, Shyam Visweswaran, George Saade, Alicia K. Smith and Ramkumar Menon\*

# Methylation differences reveal heterogeneity in preterm pathophysiology: results from bipartite network analyses

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## Abstract

**Background:** Recent studies have shown that epigenetic differences can increase the risk of spontaneous preterm birth (PTB). However, little is known about heterogeneity underlying such epigenetic differences, which could lead to hypotheses for biological pathways in specific patient subgroups, and corresponding targeted interventions critical for precision medicine. Using bipartite network analysis of fetal DNA methylation data we demonstrate a novel method for classification of PTB.

**Methods:** The data consisted of DNA methylation across the genome (HumanMethylation450 BeadChip) in cord blood from 50 African-American subjects consisting of 22 cases of early spontaneous PTB (24–34 weeks of gestation) and 28 controls (>39 weeks of gestation). These data were analyzed using a combination of (1) a supervised method to select the top 10 significant methylation sites, (2) unsupervised “subject-variable” bipartite networks to visualize and quantitatively analyze how those 10 methylation sites co-occurred across all the subjects, and across only the cases with the goal of analyzing subgroups and their

underlying pathways, and (3) a simple linear regression to test whether there was an association between the total methylation in the cases, and gestational age.

**Results:** The bipartite network analysis of all subjects and significant methylation sites revealed statistically significant clustering consisting of an inverse symmetrical relationship in the methylation profiles between a case-enriched subgroup and a control-enriched subgroup: the former was predominantly hypermethylated across seven methylation sites, and hypomethylated across three methylation sites, whereas the latter was predominantly hypomethylated across the above seven methylation sites and hypermethylated across the three methylation sites. Furthermore, the analysis of only cases revealed one subgroup that was predominantly hypomethylated across seven methylation sites, and another subgroup that was hypomethylated across all methylation sites suggesting the presence of heterogeneity in PTB pathophysiology. Finally, the analysis found a strong inverse linear relationship between total methylation and gestational age suggesting that methylation differences could be used as predictive markers for gestational length.

**Conclusions:** The results demonstrate that unsupervised bipartite networks helped to identify a complex but comprehensible data-driven hypotheses related to patient subgroups and inferences about their underlying pathways, and therefore were an effective complement to supervised approaches currently used.

**Keywords:** Bipartite networks; epigenetics; network analysis; preterm; visual analytics; visualization.

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\*Corresponding authors: **Suresh K. Bhavnani**, Institute for Translational Sciences, University of Texas Medical Branch, 301 University Blvd, 6.168 Research Building 6, Galveston, TX, USA, E-mail: skbhavnani@gmail.com; and **Ramkumar Menon**, Department of Obstetrics and Gynecology, Division of Maternal Fetal-Medicine Perinatal Research, The University of Texas Medical Branch, MRB 11.138, 301 University Blvd, Galveston, TX 77555, USA, E-mail: ram.menon@utmb.edu

**Bryant Dang and Maria Caro:** Institute for Translational Sciences, University of Texas Medical Branch, Galveston, TX, USA

**Varun Kilaru and Alicia K. Smith:** Department of Psychiatry and Behavioral Sciences, Emory University School of Medicine, Atlanta, Georgia

**Shyam Visweswaran:** Department of Biomedical Informatics, University of Pittsburgh, Pittsburgh, PA, USA

**George Saade:** Department of Obstetrics and Gynecology, Division of Maternal Fetal-Medicine Perinatal Research, University of Texas Medical Branch, Galveston, TX, USA

## Introduction

An estimated 13 million children are born annually through preterm deliveries, accounting for 9.6% of all births worldwide [1]. Preterm births (PTB; <37 weeks of gestation) account for approximately 70% of infant mortality and morbidity resulting in high personal and financial costs [1]. For example, compared to children born at

term, those born preterm have a higher incidence of conditions such as cerebral palsy, sensory deficits, learning disabilities, and respiratory illnesses [2]. Furthermore, as preterm children tend to have reduced fetal growth and numerous adverse intrauterine conditions, they are highly prone to the late onset of chronic diseases such as diabetes, hypertension, coronary heart disease, and stroke [3, 4]. Being born preterm therefore not only imparts a difficult start to life, but also confers considerable risk for a disease-burdened life [2–6].

What causes PTBs, and how can they be prevented? Reviews on this topic (e.g. [7]) cite numerous studies which have identified risk factors for PTB including socioeconomic status [8, 9], pre-existing comorbidities [10, 11], and smoking [12] that predispose a mother to a PTB. For example, African-American women have approximately twice the risk of PTB compared to other races [13]. However, given the narrow window of the gestation period, few of these risk factors can be easily modified, and therefore do not provide practical targets for effective and timely interventions.

Recent studies [14–16] have begun to focus on the genetic and epigenetic changes that could be implicated in triggering preterm deliveries, and which could potentially provide more practical targets for preventing them. As these studies have suggested the existence of epigenetic components in the biological pathways that trigger PTB, we recently analyzed methylated sites in fetal leukocyte DNA using whole genome analysis of cord blood from mothers who had early spontaneous PTB (gestational age 24–34 weeks) with intact membranes [16]. Methylated sites are locations on the DNA where methyl groups are added to the DNA, resulting in modification in the function of genes. In humans, DNA methylation typically occurs where a cytosine nucleotide occurs next to a guanine nucleotide (often referred to as a CpG site). Our analysis identified more than 9000 differentially methylated sites representing several potential pathophysiologic pathways including inflammation, oxidative stress, matrix metabolisms, and myometrial activation. While such studies have proposed several biological pathways, little is known about how they trigger early spontaneous PTB with intact membranes.

One possible limitation of many such studies is that they have used primarily supervised methods to conduct a univariable analysis of the genes or methylation sites. Such methods typically generate a list of significant methylated sites (after correcting for multiple testing) based on their differential methylation levels between cases and controls. While such univariable analyses are powerful for narrowing genome-wide data to a small set of significant methylation sites, the methods potentially conceal patient

subgroups that share similar methylation profiles caused by underlying molecular heterogeneity. Identifying and comprehending such patient subgroups based on their methylation profiles could enable inference for pathways triggering PTBs in each subgroup. Such results are a critical step in the design of targeted interventions, a cornerstone of precision medicine.

One promising approach for identifying and comprehending such complex patterns of co-occurrence is through unsupervised bipartite network analysis [17]. For example, we have demonstrated that subject-variable bipartite networks [18] (which represent both subjects and variables in the same representation) can enable (1) the rapid identification of significant patient subgroups, and the variables (e.g. genes) that are strongly associated with them, and (2) the comprehension of those relationships resulting in hypotheses for processes (e.g. biological mechanisms) underlying those subgroups. Here we demonstrate the use of bipartite network analysis and visualization for re-analyzing data from our previous study [16] with the goal of enabling new insights into molecular heterogeneity and potential mechanisms that underlie PTB.

We begin by briefly describing current methods that have been used to identify patient subgroups in biomedical data, and our motivation for using bipartite networks to analyze subgroups based on PTB methylation. Next, we describe our network-based analytical method and how it enabled a domain expert in PTB to rapidly arrive at a complex but comprehensible understanding of heterogeneity in cases and in controls, in addition to heterogeneity within the cases which could be critical to the design of future targeted interventions. We conclude with a discussion on why subject-variable bipartite networks enabled a deeper comprehension of the data, resulting in data-driven hypotheses about the mechanisms underlying PTB.

## The role of bipartite networks in identifying and comprehending patient subgroups and underlying mechanisms

### Current approaches for identifying patient subgroups

A patient subgroup is defined as a subset of patients drawn from a population (e.g. PTB patients) that share one or more characteristics (e.g. a combination of methylation

sites). Patients have been divided into subgroups by using (a) investigator-selected variables such as using race for developing stratified regression models [19], or assigning patients to different arms of a clinical trial, (b) existing classification systems such as by using the Medicare Severity-Diagnosis Related Group (MS-DRG) [20] to assign patients into a disease category for purposes of billing, or (c) computational methods such as classification [21–23] and clustering [24, 25] to discover patient subgroups from data.

One of the simplest unsupervised methods for computationally identifying patient subgroups is by enumerating conjunctions of variables, such as by analyzing all dyads and triads of co-occurring comorbidities in the Medicare database [26], and then examining the most prevalent subgroups. Other methods attempt to partition a dataset of patients and characteristics into sets that are relatively homogenous. These sets can either be one-sided clusters (clusters of patients, or clusters of characteristics) or co-clusters [25, 27, 28] (clusters of patients and characteristics). K-means and hierarchical clustering [23, 25] are among the most commonly used one-sided clustering methods and require inputs such as a similarity measure (e.g. Jaccard similarity) and the expected number of subgroups, but with no agreed-upon approaches to automatically determine them. More recently, co-clustering [25, 27, 28] methods (also called biclustering methods) have been developed to automatically identify non-overlapping or overlapping submatrices consisting of both patients and characteristics. Compared to the above partitioning methods that use similarity measures to identify clusters, dimensionality reduction methods attempt to find a reduced dimensional space where differences among patients is maximized. For example, principle component analysis (PCA) [23] attempts to identify principal components which are weighted combinations of characteristics along which patients have the maximum variance. The patients are projected onto a plane typically defined by the two most important principal components. Methods such as k-means are then used to identify clusters of patients in this reduced dimensional space.

In contrast to the above unsupervised methods, supervised methods focus on identifying patient subgroups by taking into consideration outcome variables (e.g. responders and non-responders in a treatment arm). For example, classification and regression trees (CART) [23] (and enhancements such as random forests [29] and bump hunting [22]) progressively divides patients into subgroups based on the outcome variable by using conjunctions of patient characteristics at each step. The

method outputs a tree, and each path from the root node to a leaf node defines a patient subgroup.

## Strengths and limitations of existing methods

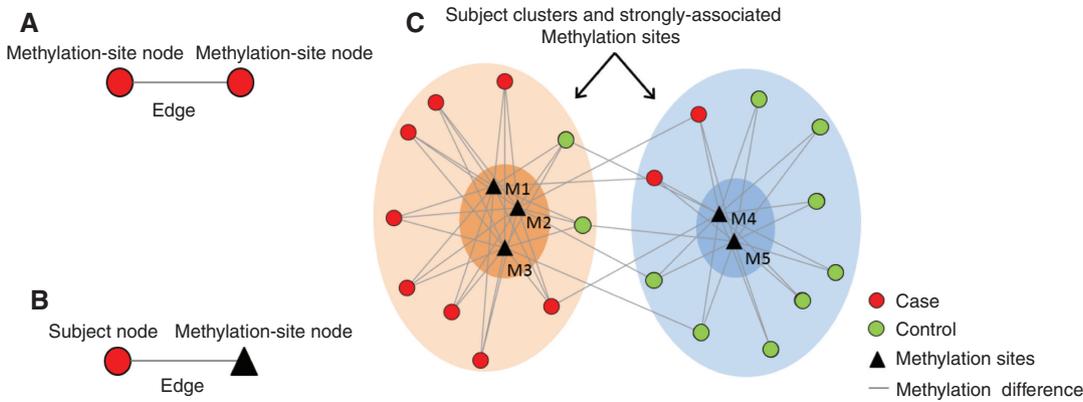
Although the above methods have improved our understanding of heterogeneity in different populations, they have important limitations with respect to enabling the identification and comprehension of patient subgroups. While all share the goal of identifying patient subgroups based on characteristics, they either (a) consider only some characteristics at a time when defining subgroups (e.g. methods using variable conjunctions), (b) output one-sided clusters such as patient subgroups without their characteristics (e.g. k-means, hierarchical clustering, PCA), or (c) cannot reveal the relationship among patient subgroups (e.g. co-clustering, CART).

As stated in the introduction, a central goal of precision medicine is not only to identify patient subgroups, but also to enable stakeholders to comprehend the processes underlying those subgroups. This comprehension of disease processes underlying patient subgroups enables stakeholders to design interventions that are targeted for each subgroup.

## Bipartite network analysis and visualization

One approach that achieves the goals of analysis and comprehension of multivariable relationships is unsupervised bipartite networks [17]. Network visualization and analysis [17] is an advanced form of visual analytics defined as “the science of analytical reasoning facilitated by interactive visual interfaces” [30]. Visual analytical methods such as unsupervised network analysis are designed to augment cognitive reasoning by transforming symbolic and numeric data into visualizations, which can be manipulated through interaction [30]. Networks have been used to analyze a wide range of complex clinical, molecular, and social phenomena such as the co-occurrence of multimorbidities across patients [31], protein-protein interactions [32], and the spread of infections across a social group [33].

A network (also called a graph) [17] consists of a set of nodes, connected in pairs by edges; nodes represent one or more types of entities (e.g. subjects or methylation sites). Edges between nodes represent a specific relationship between the entities (e.g. a subject has a specific methylation difference at a methylation site). Figure 1A



**Figure 1:** The distinction between a unipartite network (A), a bipartite network (B), and how the latter can be used to identify clusters of subjects and strongly associated methylation sites (C).

shows a unipartite network where nodes are of the same type (commonly used to analyze co-occurrence of genes across patients, or to analyze protein-protein interaction networks [32]). In contrast, Figure 1B shows a bipartite network where nodes are of two types, and edges exist only between different types of nodes such as between subject nodes (circles) and methylation site nodes (triangles).

Networks are typically laid out using force-directed algorithms that pull together nodes that are strongly connected, and push apart nodes that are not. The result is that nodes with a similar pattern of connections are placed close to each other, and those that are dissimilar are pushed apart. As shown in Figure 1C, the application of the *Kamada Kawai* force-directed algorithm [34] to a bipartite network has revealed two clusters of subjects (one on the left and one on the right), each strongly associated with different methylation sites.

In prior work [35–40] we have shown that such “subject-variable” [18] bipartite networks are especially effective in helping to comprehend subject subgroups because they not only help to identify how subjects cluster with each other, but also how they are related to variables such as methylation sites. This feature enables an understanding of intra-cluster associations (e.g. the left cluster is enriched with cases associated predominantly with three methylation sites) and inter-cluster associations (e.g. the degree to which the subjects in the case-enriched cluster shares methylation sites with the control-enriched cluster as revealed by the inter-cluster edges). Furthermore, this feature distinguishes bipartite networks from other unsupervised methods [41] such as unipartite clustering (e.g. k-means and hierarchical clustering), and dimensionality reduction methods (e.g. principal component analysis)

that cluster either subjects or variables, but not both simultaneously.

## Methods

### Data selection

For the current study, we reanalyzed samples drawn from the Nashville Birth Cohort (NBC) described in a previous study [16]. Briefly, the NBC consists of samples of spontaneous preterm birth (cases), and of normal term birth (controls). In this cohort, maternal demographic and clinical data were recorded from medical records or through interviews during the consenting process; demographic and clinical data specific to the fetus were extracted from clinical records; gestational age of the neonate was determined by maternal reporting of the last menstrual period and corroborated through ultrasound dating; race was identified by self-reporting tracing back to three generations from the maternal and paternal sides of the fetus; and maternal self-reports were used to determine socioeconomic (education, household income, marital status, and insurance status), and behavioral (cigarette smoking) factors. A detailed description of these and other variables such as infections are described in past publications [42–44].

As described in our primary study [16], the samples used for the current analysis consisted of 50 African-American subjects of non-Hispanic ethnicity consisting of 22 cases of early spontaneous PTB (gestational age 24–34 weeks) and 28 controls (gestational age > 39 weeks). These cases and controls did not differ significantly in demographic or clinical factors [16, 45–50]. A detailed description of assay methods, analytical approaches, and data quality control measures can be accessed from the primary study [16]. To limit the influence of technical artifacts,  $\beta$  values for each methylation site were residualized to account for chip and row. Similarly, to limit sex-specific effects, the effects of sex were also residualized using a multiple regression. This retrospective study was approved by the Institutional Review Board (IRB) at the University of Texas Medical Branch. The data files used for the study were in the research identifiable format (RIF), and the records were anonymized and de-identified

prior to analysis. As analysis of such data does not require informed consent, it was therefore not done.

## Bipartite network analysis

Our analysis consisted of three steps [18]: (1) exploratory visual analysis to identify emergent bipartite relationships such as patterns of how methylation sites co-occur across subjects; (2) quantitative analysis to quantitatively verify and statistically evaluate the emergent patterns such as clusters; (3) inference of the biological mechanisms underlying different emergent clusters of subjects. This three-step method used in our earlier studies has revealed complex but comprehensible visual patterns, leading to inferences about the biomarkers and underlying mechanisms involved.

**1. Exploratory visual analysis.** We constructed two bipartite networks to analyze patient subgroups based on methylation profiles with the goal of comprehending the molecular pathways involved in PTB: (1) a case-control bipartite network of 22 cases, 28 controls, and significant methylation sites, and (2) a case-only bipartite network of only the 22 PTB cases and significant methylation sites.

Nodes in the above bipartite networks represented subjects or methylation sites. To analyze the association of subjects to methylation sites that had strong signal for PTB, we (a) ranked all methylation sites identified in our earlier study based on their univariable significance, (b) removed all methylation sites that were not on a gene, and that had a SNP under the probe, and (c) selected the top-10 ranked ( $FDR < 7.41 \times 10^{-8}$ ) methylation sites. The resulting case-control network consisted of 50 subjects (22 cases and 28 controls) and 10 methylation sites, and the case-only network consisted of 22 cases and the same 10 methylation sites. Furthermore, we used node color to distinguish cases (red) from controls (green) in the case-control network, and to distinguish emergent subgroups (case-subgroup-1 = pink, case-subgroup-2 = blue) in the case-only network.

Edge weights in the networks were used to represent the degree of methylation differences for each subject-methylation site pair. Because DNA methylation was measured on different chips, and methylation is already known to be strongly associated with gender of the fetus, the  $\beta$  values for each methylation site were residualized to account for chip, row, and sex-specific effects using a multiple regression. As regression residuals can range from negative to positive, and network layout algorithms require positive distances to position nodes, we shifted all residual values into the positive range. This was done by adding the least residual value for each methylation site to all its values, an approach which preserved the relative distances between subjects, and therefore enabled laying out the network using a standard force-directed algorithm.

Global patterns related to subjects and variables in the network were visualized and analyzed using the *Kamada-Kawai* [34] layout algorithm in Pajek (version 3.02) [51]. As shown in Figure 1C, the algorithm pulls together nodes that are strongly connected, and pushes apart nodes that are not. This algorithm is fast but approximate and is well-suited for medium sized networks consisting of between 100 and 1000 nodes [51]. The result is that nodes with a similar pattern of connections (e.g. M1 and M2 strongly associated with the left cluster in Figure 1C) are placed close to each other.

A key advantage of a bipartite network representation is the simultaneous visualization of subjects and variables, relationships between them (methylation differences), node type (cases and controls), and emergent global patterns (clusters) in a uniform visual representation. Such a representation enables domain experts such as clinicians and biologists to comprehend explicit associations such as how subject nodes are connected to methylation site nodes, in addition to emergent associations such as intra and inter cluster associations, leading to the rapid generation of hypotheses based on complex multivariable relationships.

**2. Quantitative analysis.** We used three measures to quantitatively verify and statistically evaluate patterns derived from the exploratory visual analysis. These methods were selected based on their appropriateness to the emergent patterns in the network.

(a) **Agglomerative hierarchical clustering:** Because the network layout suggested a clustered topology for subjects and for methylation sites, we used the agglomerative hierarchical clustering method [41], which is best suited for networks that have small clusters [18, 35]. The clustering was done using the Manhattan dissimilarity measure with the Ward linkage function, and the number of clusters and their boundaries were determined based on natural breaks in the subject and methylation site dendrograms. The dendrograms were also combined with the heatmaps to aid in the visual analysis of the results.

(b) **Clusteredness:** To test whether the clusters in the network could have occurred by chance, we compared the variance, skewness, and kurtosis of the dissimilarities in the data, to 1000 random permutations of the dataset. For each network permutation, we preserved the size of the network, in addition to the edge weight distribution across patients when analyzing the patient dendrogram, and the edge weight distribution across methylation sites when analyzing the methylation dendrogram. Significant breaks in the subject or methylation site dendrograms would result in a significantly larger variance, skewness, and kurtosis of the dissimilarity measures, compared to the same measures generated from random permutations of the networks. Furthermore, we tested whether the proportion of cases and controls in the emergent subject clusters were significant using the  $\chi^2$  test.

(c) **Association between methylation and gestational age:** As the two clusters of nodes in the case-only network appeared to have a wide range in methylation differences, we used simple linear regression to test whether there was an association between total methylation of each subject, and gestational age. This was done by calculating the weighted degree centrality [17] for each patient node (sum of all its methylation differences across all the methylation sites), and testing its association (binned in increments of 0.25) to gestational age.

**3. Inference of biological mechanisms.** The verified clusters of subjects and methylation sites were used to identify hypotheses for biological pathways. This was done by (a) identifying the methylation sites that were strongly associated with each subject cluster, (b) mapping the methylation sites to their respective genes, and (c) identifying the biological pathways that are represented by the differentially methylated genes through the use of ingenuity pathway analysis (IPA). IPA (Ingenuity® Systems www.ingenuity.com) is a widely used database and retrieval system designed to help researchers map a given set of molecules to biological pathways published in the literature.

## Results

The bipartite network analyses revealed distinct patterns of methylation differences between cases and controls, in addition to distinct patterns of methylation differences between subsets of cases.

### DNA methylation differences between cases and controls

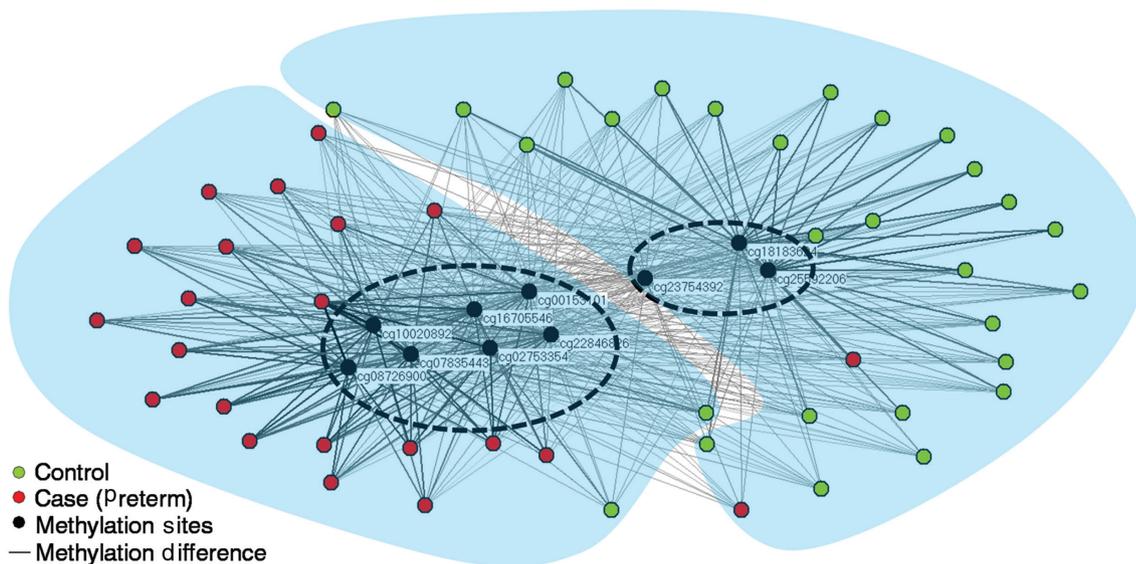
The bipartite network visualization of 50 subjects (22 cases and 28 controls), and 10 methylation sites revealed a complex but understandable clustered pattern. As shown in Figure 2, there were two major clusters of subjects and methylation sites, one to the left, and another to the right.

To quantitatively verify the number of clusters and their members, we used agglomerative hierarchical clustering for the subjects, and for the methylation sites. As shown in Figure 3, the dendrogram shows a substantial break at two clusters both for the subjects, and for the methylation sites. The clusteredness of the subjects in the case-control network was statistically significant when compared to 1000 random permutations of the networks based on variance of the dissimilarities (case-control network=9.25, random mean=1.09,  $P < 0.001$  two-tailed test), skewness of the distribution of dissimilarities (case-control network=6.06, random mean=2.77,  $P < 0.001$  two-tailed test), and

kurtosis of the distribution of dissimilarities (case-control network=40.08, random mean=12.40,  $P < 0.001$  two-tailed test). Similarly, the clusteredness of the methylation sites in the case-control network was also statistically significant when compared to 1000 random permutations of the networks based on variance of the dissimilarities (case-control network=38.01, random mean=3.61,  $P < 0.001$  two-tailed test), skewness of the distribution of dissimilarities (case-control network=2.32, random mean=-0.24,  $P < 0.001$  two-tailed test), and kurtosis of the distribution of dissimilarities (case-control network=6.68, random mean=1.89,  $P < 0.001$  two-tailed test).

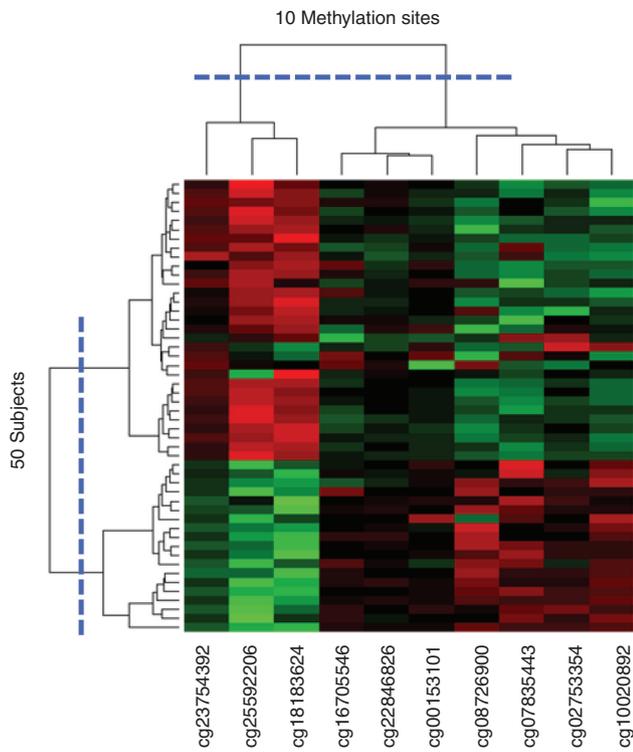
The cluster boundaries of subjects were superimposed onto the network using translucent blue shapes, and the cluster boundaries of methylation sites were superimposed on the network using dashed ovals. This superimposition of cluster boundaries on the network revealed that the subject cluster on the left contained mainly cases, but also included two controls; the subject cluster on the right had mainly controls, but also included two cases. Despite this cross-over of phenotypes, the proportion of cases and controls in each subject cluster was significantly different ( $\chi^2$  Yates (1,  $n = 50$ ) = 35.0757,  $P < 0.001$ ), suggesting an overall strong separation in cases and controls based on their methylation profiles.

The subjects in the left case-dominated cluster (red nodes) were hypermethylated at seven methylation sites and their respective genes: cg10020892 (*BCL9*), cg22846836 (*FO XK1*), cg08726900 (*ANKRD11*), cg02753354



**Figure 2:** Bipartite network visualization of 50 subjects (22 cases, 28 controls) and methylation sites.

The network revealed a significant separation between cases and controls, and the methylation sites that were strongly associated with each cluster. The blue shapes and dashed ovals denote cluster boundaries of subjects and methylation sites, respectively identified through agglomerative hierarchical clustering.



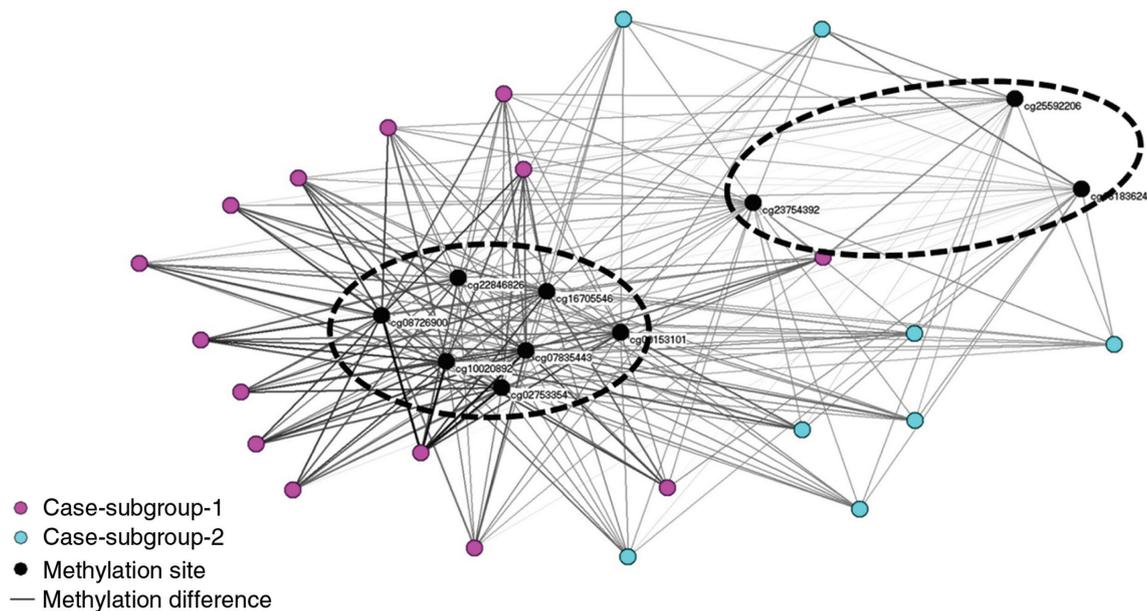
**Figure 3:** Heatmap with dendrograms of 50 subjects and 10 methylation sites generated through agglomerative hierarchical clustering. The largest break in the dendrogram is shown with the blue dotted lines, resulting in two clusters of methylation sites, and two clusters of subjects.

(*HMHA1*), cg07835443 (*C16orf55*), cg16705546 (*IRF8*), cg00153101 (*PLCH2*). They were also hypomethylated at the following three methylation sites and their respective genes: cg23754392 (*BMI1*) and cg25592206 (*CDKN2C*), and cg18183624 (*IGF2BP1*). In contrast, the subjects in the right control-dominated cluster (green nodes) had the opposite pattern: the subjects were hypomethylated at the above seven methylation sites, and hypermethylated at the above three methylation sites.

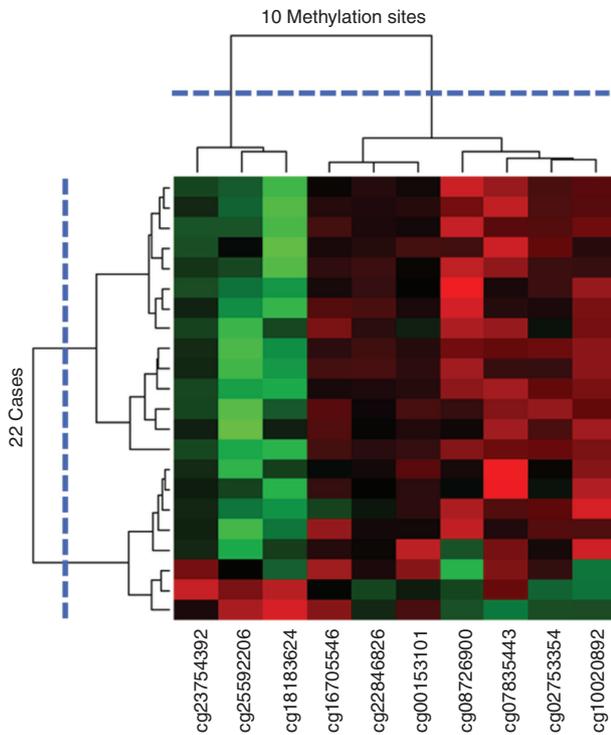
**DNA methylation differences among cases**

Because there was an overall strong and significant separation of cases from controls, this separation could have concealed sub-patterns within the cases. We therefore removed all the controls from the network to inspect possible patterns among only the cases. Figure 4 shows the resulting network of 22 cases and the 10 methylation sites which was laid out and analyzed using the same approach as was used for the previous case-control network.

As shown in Figure 4, there was a cluster of cases on the left that was strongly hypermethylated at the same seven methylated sites as in the case-control network. However, as shown on the right, there was a dispersed group of cases with mainly thin edges connecting them to all the methylation sites, suggesting that this subgroup was hypomethylated at all the 10 methylation sites.



**Figure 4:** Bipartite network visualization of 22 cases and 10 methylation sites. The network revealed two clusters of cases, and the methylation sites that were strongly associated with each. The dashed ovals denote boundaries of case clusters identified through agglomerative hierarchical clustering.



**Figure 5:** Heatmap with dendrograms of 22 cases and 10 methylation sites generated through agglomerative hierarchical clustering. The largest break in the dendrogram is shown with the blue dotted lines, resulting in two clusters of methylation sites, and two clusters of cases.

Similar to the previous analysis, we quantitatively determined the boundaries of the clusters in the case-only network through agglomerative hierarchical clustering for the subjects and for the methylation sites. As shown in Figure 5, the dendrogram showed a substantial break at two clusters both for the subjects, as well as for the methylation sites. The cluster boundaries of the subjects were superimposed on the network using node color, and the cluster boundaries of the methylation sites were superimposed on the network using dashed ovals.

The clusteredness of the subjects in the case-only network was statistically significant when compared to 1000 random permutations of the network based on variance of the dissimilarities (case-only network=1.31, random mean=0.89,  $P < 0.001$  two-tailed test), skewness of the distribution of dissimilarities (case-only network=2.80, random mean=1.60,  $P < 0.001$  two-tailed test), and kurtosis of the distribution of dissimilarities (case-control network=10.47, random mean=5.20,  $P < 0.001$  two-tailed test). Similarly, the clusteredness of the methylation sites in the case-only network was also statistically significant when compared to 1000 random permutations of the network based on variance

of the dissimilarities (case-only network=10.05, random mean=3.76,  $P < 0.001$  two-tailed test), skewness of the distribution of dissimilarities (case-only network=2.30, random mean=1.96,  $P < 0.001$  two-tailed test), and kurtosis of the distribution of dissimilarities (case-only network=6.62, random mean=5.66,  $P < 0.001$  two-tailed test). These results suggest the existence of two PTB subgroups. The first subgroup on the left was hypermethylated at seven sites, and hypomethylated at three sites. In contrast, the second subgroup on the right was hypomethylated on all 10 sites.

In summary, the bipartite network visualizations and analyses led to two key findings. (1) There existed an inverse symmetrical relationship in the methylation profiles between the cases and controls: cases were predominantly hypermethylated at seven methylation sites, and hypomethylated at three methylation sites, whereas controls were predominantly hypomethylated at the above seven methylation sites and hypermethylated at the above three methylation sites. (2) There was strong evidence for heterogeneity in the profiles of the cases, where one patient subgroup was predominantly hypermethylated across seven methylation sites, and another patient subgroup was hypomethylated across all 10 methylation sites.

## Relationship between methylation and gestational age

Because the two patient subgroups in the case-only network had a wide range in overall methylation differences, we tested if there was an association between total methylation difference in each case, and gestational age. The results showed an inverse linear relationship between the total methylation for each subject (binned in increments of 0.25), and gestational age (best fitted by  $y = -1.6222x + 36.052$ ,  $R^2 = 0.8488$ ).

## Inferences for biological mechanisms in preterm birth

An important goal of network visualization and analysis is to enable the comprehension of complex patterns in the data leading to hypotheses for the underlying processes such as biological mechanisms. Accordingly, given the significant separation of cases and controls in the case-control network, and the significant heterogeneity in the case-only network, our goal was to infer the possible biological pathways underlying those patterns. We therefore used IPA to identify known pathways related

to genes represented by the seven methylation sites, and related to the genes represented by the three methylation sites (shown on the left and the right of both networks, respectively). The two bipartite networks along with the pathways identified from IPA were provided to a domain expert in PTB, who was asked to infer the potential mechanisms leading to PTB.

For the case-control network, he first attempted to analyze the IPA-identified pathways related to the seven methylation sites that were hypermethylated in the left case-dominated cluster. Unfortunately, none of the pathways appeared to be meaningful for PTB. Next, he analyzed the IPA-identified pathways related to the three sites that were hypermethylated in the right control-dominated cluster. Here he inferred that two of the hypermethylated sites (cg23754392, cg25592206) were likely downregulating their respective genes (*BMI1* and *CDKN2C*) leading to the upregulation of *TP53* (a known tumor suppressor), resulting in normal cell senescence required for the normal rupture of the placenta during labor. Because these very methylation sites were hypomethylated (represented explicitly by the thin edges that connected most of the subjects in the left case-dominated cluster, to these two methylation sites on the right), he hypothesized that the opposite might hold for the cases: hypomethylation of the same two sites would lead to upregulation of *BMI1* and *CDKN2C*, leading to the suppression of *TP53* potentially resulting in decreased or absent cellular senescence.

Having determined a plausible role of cellular senescence in PTB, he reexamined the genes related to the hypermethylated sites in the case-dominated cluster on the left. This led to a focus on *BCL9* and *IRF8*, which he noted were both cell cycle promoters. He therefore unified the two insights by hypothesizing that the decrease or absence of the pathway related to normal cellular senescence (inferred from the methylation sites strongly associated with the control-dominated cluster on the right), in combination with the presence of the pathway that promoted cell cycle (inferred from the methylation sites strongly associated with the case-dominated cluster on the left) might potentially be responsible for triggering PTB in the cases.

Next, he attempted to infer the plausible mechanisms underlying the heterogeneity in the case-only network (Figure 4). As the left subgroup had mostly uniform hypermethylation of seven sites and hypomethylation of three sites, he inferred that the mechanisms underlying this subgroup also related to senescence. In contrast, as the right subgroup had mostly uniform hypomethylation of all 10 sites, he inferred that while they did not have a

strong signature for senescence like the left subgroup, they also did not have as strong a signature as that of the control-dominated subgroup identified in Figure 3. This implied the existence of a continuum in methylation profiles, which could be the result of interaction with other risk factors triggering a PTB. Furthermore, the inverse relationship between total methylation and gestational age suggested that the fetal methylation associated epigenetic signature may be a useful predictor of an adverse pregnancy outcome such as PTB.

Recent studies provide corroborative evidence for the above mechanistic inferences. For example, existence of senescence as a mechanism was recently reported in fetal membranes and in fetal DNA [52–55]. However, because the precise mechanisms or functional pathways cannot be identified from differential methylation profiling, additional functional studies need to be conducted on these identified genes. Furthermore, methylation differences (hyper or hypo) are not always unidirectional [14], and many of the functional changes are linked to the type of cell or tissue, and the environment to which they are associated. Therefore, while the above inferences of pathways and heterogeneity derived from the visual analytics provide promising hypotheses related to senescence of fetal cells, these results need to be closely examined through future hypothesis-testing studies.

## Discussion

From a biological perspective, even though the data had been previously rigorously analyzed, both networks revealed complex but comprehensible patterns leading to novel data-driven hypotheses. The case-control network revealed an inverse symmetrical relationship between cases and controls leading to biological inferences related to senescence. Furthermore, as discussed in the methods section, we used stringent criteria for the inclusion and exclusion of subjects, resulting in a relatively homogeneous group of cases and of controls with no significant demographic and clinical differences between them. However, despite these stringent criteria, the case-only network revealed patient subgroups based on methylation differences alone, demonstrating the important role that methylation changes in fetal DNA can play in revealing meaningful heterogeneities among cases.

From a methodological perspective, there were four features of the network representation that together contributed to the rapid inferences related to the pathophysiology in preterm births:

1. **Representation of node similarity in a Euclidean plane.** Because a force-directed algorithm positions nodes in a Euclidean plane, it can use two degrees of freedom and continuous distances to more accurately represent inter-node similarity. For example, in a Euclidean plane, a node can have an identical relationship to many other nodes simultaneously. This feature enabled the rapid detection of node associations such as clusters in both networks, in addition to revealing the degree of similarity of nodes within each cluster in the case-only network. In contrast, heatmaps (Figures 3 and 5) position all nodes along a line either on the x- or y-axes at discrete distances determined by the widths of the rows and columns, which constrains how distance can be used to represent similarity between nodes. For example, a node can have an identical distance to a maximum of two nodes (one on either side), making it more difficult to accurately represent and comprehend complex inter- and intra-cluster relationships. Therefore, while heatmaps are useful for verifying patterns once identified, bipartite networks laid out in a Euclidean plane are more effective to support the process of discovery and inference of inter-node associations between and within clusters [35].
2. **Representation of subjects and variables using two sets of nodes.** Because we represented subjects and variables simultaneously in the network, they helped to comprehend inter and intra cluster relationships. This feature facilitated the inspection of which subject clusters were or were not strongly associated with which methylation clusters enabling inference of pathways.
3. **Representation of subject type using node color.** Because we chose to distinguish cases and controls in the case-control network by coloring them red and green respectively, they enabled rapid detection of the composition of clusters. This feature resulted in the identification of a case-dominated cluster, and a control-dominated cluster in the case-control network.
4. **Representation of variable values using continuous edge thickness.** Because we chose to represent variable values as edge thicknesses, they enabled comprehension of the strength of associations within and across clusters. This feature enabled detection of hypo- and hypermethylation associations within and between clusters in both networks.

While each of the above representational features made specific contributions to the comprehension of the data, it is their *simultaneous* visualization which enabled the complex inference of the underlying biology. Therefore, while the network topology with two subject and two

methylation site clusters looked deceptively simple, the combination of the above four representational features precipitated a plausible hypothesis of mechanisms and heterogeneity in PTB. Such a result would be difficult to derive if we had used only supervised methods such as univariable significance of the methylation sites, or by just analyzing a textual description of node membership in subject and methylation clusters.

The above process of comprehending visual patterns and inferring their meaning is based on well-known cognitive processes related to information visualization. Cognitively, visualizations such as subject-variable networks map multiple data elements to externalized visual representations. When this mapping to visual elements is aligned with cognitive principles [30, 56–59], the resulting visual representation enables comprehension of complex patterns because of two key cognitive processes: (1) The visual representation leverages the massively parallel architecture of the human visual system consisting of the eye and the visual cortex of the brain [56]. This parallel cognitive architecture enables the rapid comprehension of multiple graphical elements simultaneously, which often leads to insights about relationships in complex data such as similarities, trends, and anomalies [30]. (2) The externalized representation reduces working memory load needed to process the data [60], enabling the freed-up working memory to be used for higher-level processing such as the interpretation of patterns, requiring access of domain-knowledge in long-term memory.

Furthermore, while visualizations enable rapid comprehension of associations that are made explicit by the nodes, edges, and their properties, they also enable detection of implicit associations [61] resulting from the layout in an Euclidean plane including emergent multivariable patterns such as clusters. As demonstrated in the current analyses, these cognitive advantages conferred by appropriately designed subject-variable networks are critical for projects at early stages of discovery (such as the epigenetic analysis of PTB) as they enable complex reasoning about subjects and the variables. Often this process results in the discovery of novel multivariable patterns in the data [35–40], such as heterogeneity based on methylation differences, and hypotheses for their underlying mechanisms, an early but crucial step in the design of targeted interventions.

## Conclusion

Although several studies have analyzed epigenetic changes in preterm, little is known about the mechanisms

that trigger PTB. Here we demonstrated how bipartite networks revealed an inverse symmetrical relationship in the methylation profiles between PTB cases and controls, resulting in a complex but comprehensible hypothesis of the mechanisms precipitating PTB. Furthermore, the analysis revealed statistically significant heterogeneity within the methylation profiles of PTB cases, which is an early step towards the design of targeted interventions, a critical goal of precision medicine.

Although we do not yet know how methylation affects the function of genes involved in PTB, our analysis suggests distinct mechanisms of PTB that involve the presence or absence of senescence. These pathways are most likely mediated by exposure to different risks which can impact methylation patterns leading to PTB. Bipartite network analyses therefore enabled us to derive data-driven hypotheses of pathways in PTB, which should be tested in future functional methylation studies. Our current research focuses on extending the subject-variable network analysis approach to process big datasets consisting of thousands of subjects and variables.

The limitation of this study is that our samples were derived from cord blood, and therefore the data cannot be used to establish causation based on fetal DNA methylation patterns at the time of birth. Accordingly, in our future work we will use maternal samples and prospective samples through which we will test the validity of our approach to further delineate cause and effect in patient subgroups, with the ultimate goal of developing targeted interventions to reduce the risk of preterm deliveries.

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#### Author's statement

**Conflict of interest:** Authors state no conflict of interest.

**Material and methods:** Informed consent: Informed consent has been obtained from all individuals included in this study.

**Ethical approval:** The research related to human subject use has complied with all the relevant national regulations, and institutional policies, and is in accordance with the tenets of the Helsinki Declaration, and has been approved by the authors' institutional review board or equivalent committee

**Author contributions:** Conceived and designed the analysis: SKB BD RM. Extracted the data: RM VK. Analyzed the data: SKB BD VK AKS. Wrote the paper: SKB BD VK MC SV GS SEP AKS RM.

**Data availability:** The data used in this study were extracted from epigenetic studies conducted by Dr. Menon

(ram.menon@utmb.edu), and Dr. Smith (alicia.smith@emory.edu). These data can be obtained through email request.

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